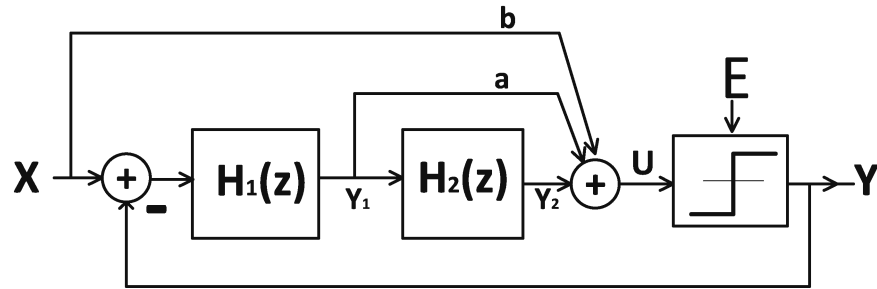


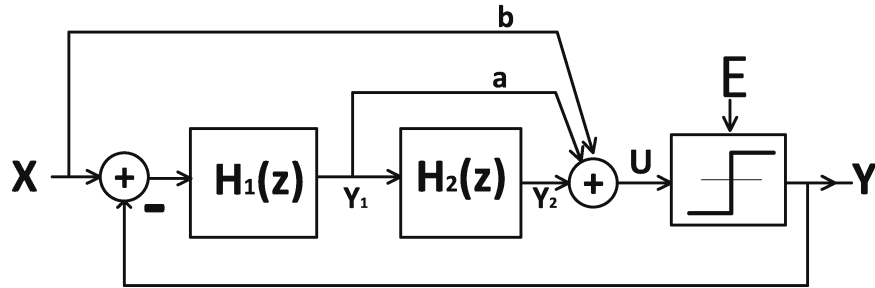
Sample Exam ECE 428/528

Final

2(a) For the feedforward delta-sigma loop, find “b” such that the signal transfer function is 1.

2(b) Find “a” such that for $H_1(z)=H_2(z)=(z-1)^{-1}$, the noise transfer function is $(1-z^{-1})^2$.





$$H_1(z) = H_2(z) = z^{-1}/(1-z^{-1})$$

$$Y_1 = U_1(X - Y)$$

$$Y_2 = H_1 H_2 (X - Y)$$

$$U = bX + aY_1 + Y_2 = bX + (a + H_2)H_1(X - Y)$$

$$U = [b + (a + H_2)H_1]X - (a + H_2)H_1Y = Y - E$$

$$[1 + (a + H_2)H_1]Y = [b + (a + H_2)H_1]X + E \quad \therefore b = 1 \text{ for unity transfer function}$$

$$Y = X + E / [] \quad \therefore 1/[] = 1/(1 + aH_1 + H_1^2) = (1 - z^{-1})^2 / ((1 - z^{-1})^2 + az^{-1}(1 - z^{-1}) + z^{-2})$$

The denominator is:

$$1 - 2z^{-1} + z^{-2} + az^{-1} - az^{-2} + z^{-2} = 1 \Rightarrow a = 2$$